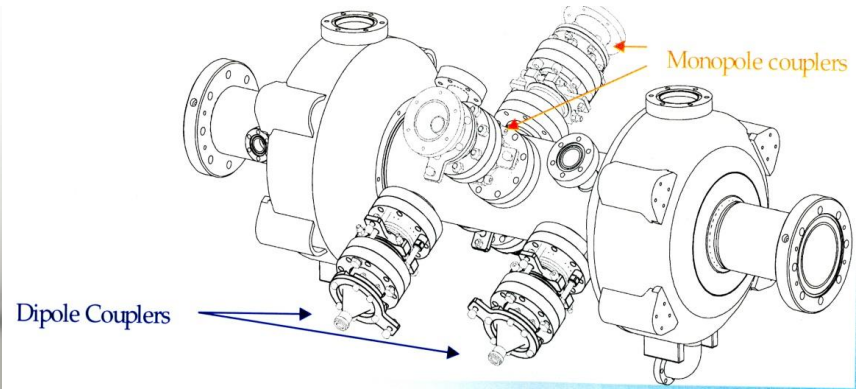
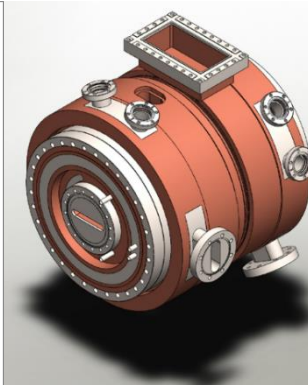
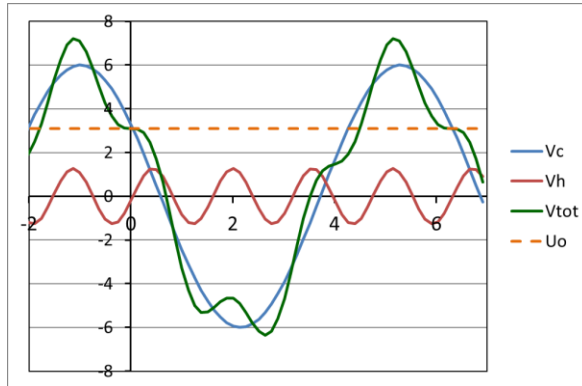


Passive vs Active Systems, DC Robinson, DLLRF

Jörn Jacob



HARMONIC RF FOR BUNCH LENGTHENING

$$V_{\text{acc}}(\phi) = V_c \sin(\phi_s + \phi) + V_h \sin(n\phi_h + n\phi)$$

Optimum Working point (1st & 2nd derivatives = 0):

$$\phi_s = \pi - \arcsin[n^2/(n^2-1) U_0/V_c]$$

$$V_{h,\text{opt}} = \text{sqrt}[V_c^2/n^2 - U_0^2/(n^2-1)]$$

$$\phi_{h,\text{opt}} = (1/n) \arcsin[- U_0 / (V_{h,\text{opt}} (n^2-1))]$$

For instance 4th harmonic RF for the ESRF:

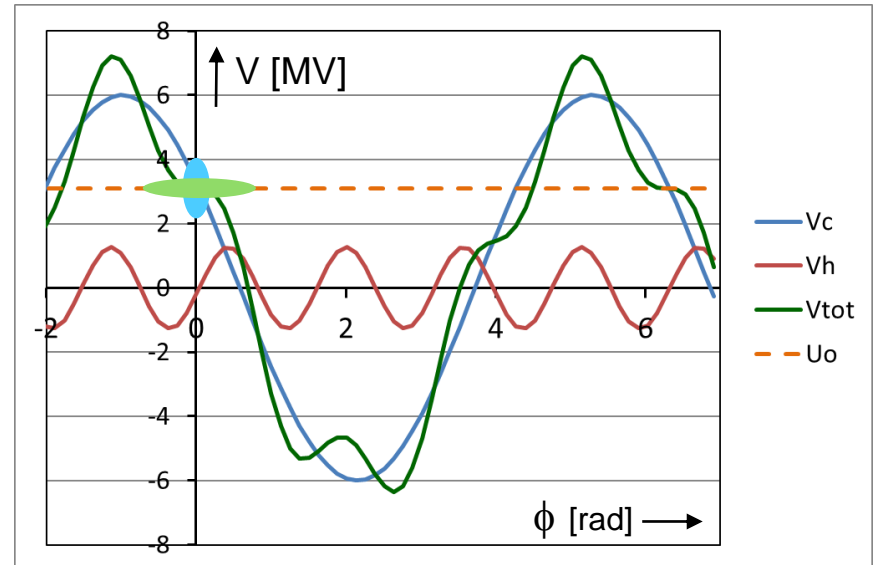
$$U_0 = 2.52 \text{ MeV / turn (without ID = worst case)}$$

$$V_c = 6.0 \text{ MV}$$

$$\phi_s = 153.38 \text{ deg}$$

$$V_{h,\text{opt}} = 1.35 \text{ MV}$$

$$n\phi_{h,\text{opt}} = -7.14 \text{ deg}$$



Principle: 4th harmonic RF system for bunch lengthening

Passive NC harmonic cavity :

- ✓ MAXIV, Solaris: 3 x 100 MHz
- ✓ ALS: 3 x 500 MHz
- ✓ BESSY: 3 x 500 MHz

Pros:

- Simple, most economic solution
- V_h driven by the beam
- Only f_{res} tuning to obtain desired $V_h = f(I_{\text{beam}})$
- V_h phase follows beam phase
 - ⇒ no phase tuning required
 - ⇒ no DC Robinson problem

Cons:

- Low total impedance → only for high current operation
- Low Q → $V_{h,\text{opt}}$ achievable if enough total current, but not $\phi_{h,\text{opt}}$
 - i.e.: cancelation of 1st derivative possible, but not 2nd derivative
 - nevertheless, significant bunch lengthening achievable
- High total R/Q → Strong phase transients ~ R/Q

Passive SC harmonic cavity :

- ✓ SLS, Elettra: 3 x 500 MHz
- ✓ APS: 4 x 352.2 MHz, under development
- ✓ SOLEIL II: possibly

Pros:

- Almost purely inductive,
 - ⇒ $\phi_h = 0$ close to $\phi_{h,\text{opt}}$!
 - ⇒ No beam power loading
 - ⇒ $V_{h,\text{opt}}$ easily achievable down to low beam current
- Only f_{res} tuning to obtain desired $V_h = f(I_{\text{beam}})$
- V_h phase follows beam phase
 - ⇒ no DC Robinson problem
- Note: APS project foresees power coupler to slightly load the SC cavity and achieve also $\phi_h = \phi_{h,\text{opt}}$
- Low R/Q , → minimize phase transients

Cons:

- Operation of SC-RF technology, Cryoplant
 - Operation requires more financial and manpower resources than NC cavities
 - Larger risk of down time

Active NC harmonic cavity :

- ✓ ALBA, BESSY, DESY project: 3 x 500 MHz scaling of E010 EU cavity in test at BESSY
- ✓ KEK: development of 3 x 500 MHz E020 cavity
- ✓ ESRF: development of 4 x 352.37 MHz E020 cavity

Pros:

- Any V_h and ϕ_h can easily be set for any current
- Allows bunch lengthening for high and low current / few bunch filling
- Still reasonable number of cavities
- E020 cavities: similar R/Q as SC cavities
- Real alternative to SC cavities

Cons:

- Lacking operational experience
- DC Robinson stability needs to be addressed
- Requires high power RF amplifiers

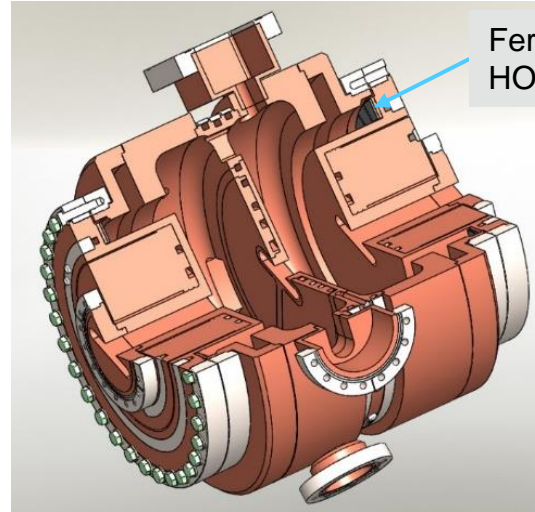
Different configurations are being evaluated by the HarmonLIP community w.r.t. stability:

- By beam tracking simulations
 - When possible: by experiments on existing systems
- See other presentations

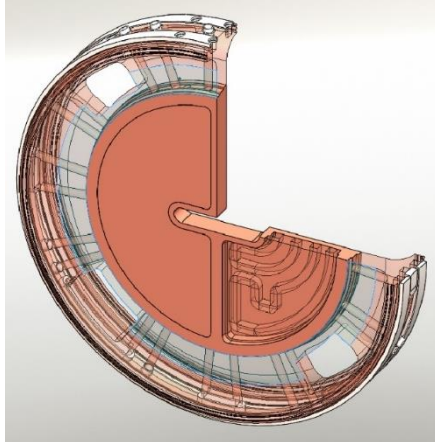
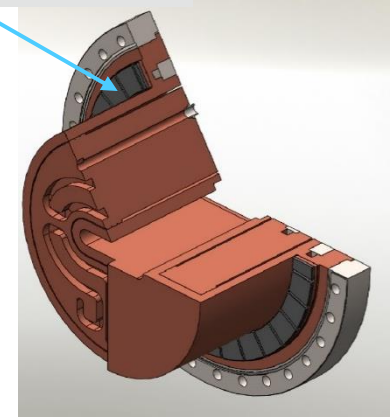
Coming slides → some considerations on:

- Robinson DC for active harmonic RF systems
- Possible active control

4TH HARMONIC 2-CELL E020 MODE CAVITY – ESRF IN HOUSE DEVELOPMENT



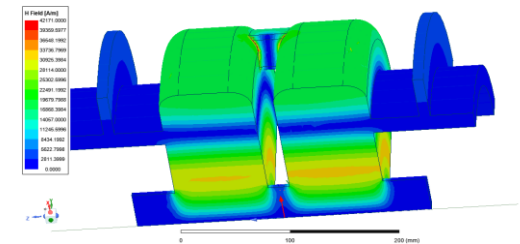
Ferrite LOM (E010 mode) & HOM absorber



Active NC cavity design well advanced:

- ✓ 2 coupled and 2 uncoupled cells considered
- ✓ Freq = 1.409 GHz
- ✓ R/Q = 44.5 ohm/cell
- ✓ Q0 = 30500
- ✓ Smart HOM & LOM dampers almost not affecting Q0 of E020 mode
- ✓ Elaborate water cooling
- ✓ Aperture coupler: **coupling $\beta = 1$**
- ✓ Vacuum ports on HOM dampers also preserving Q0

H-Field

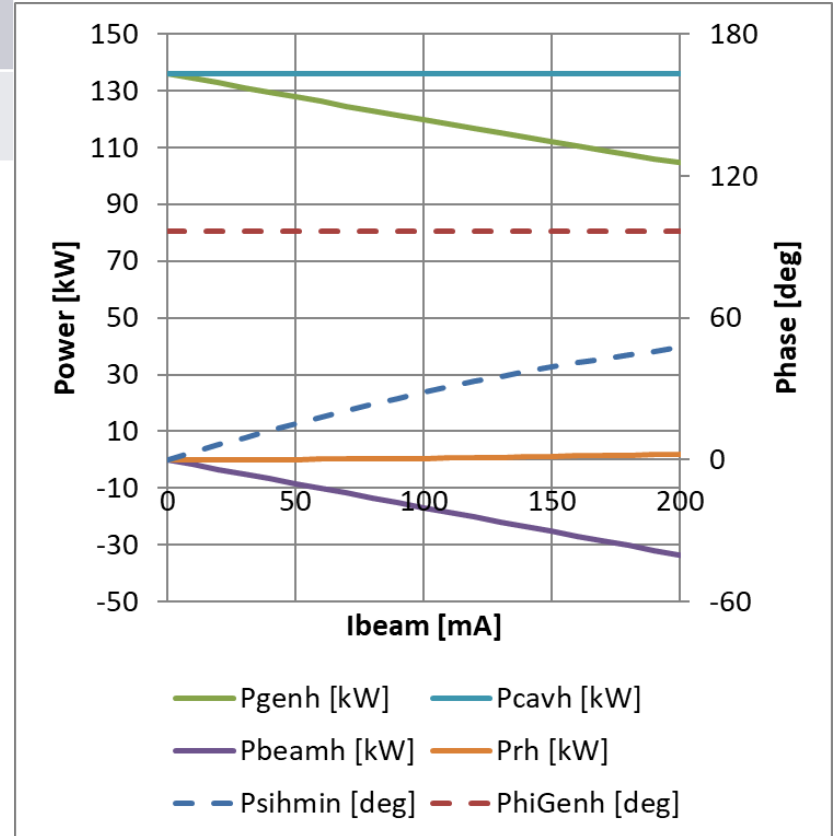
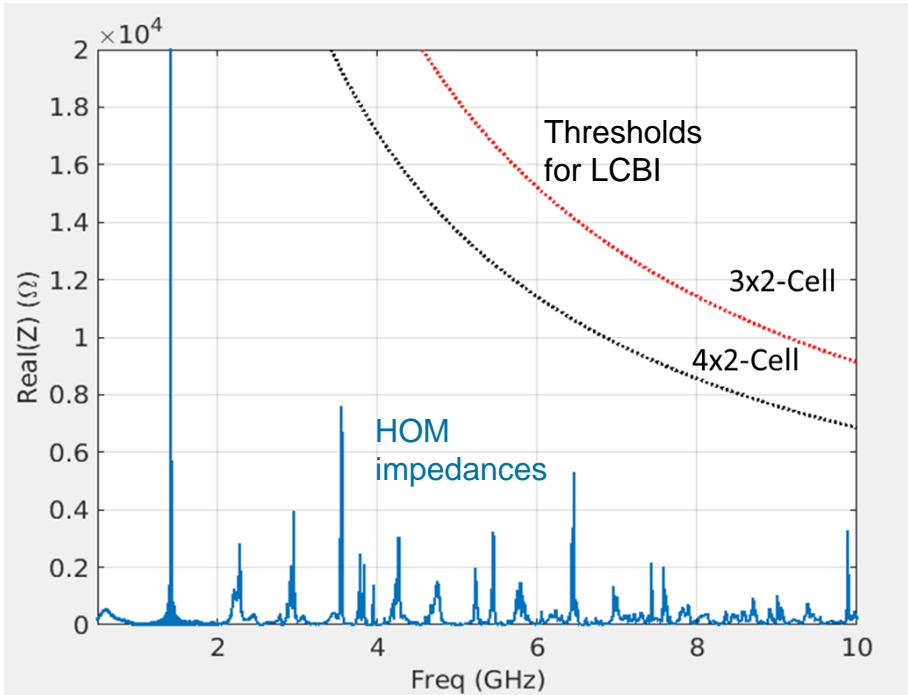


[E020 proposed by Naoto Yamamoto, KEK
ESRF design by Alex D'Elia, Vincent Serrière]

ACTIVE HARMONIC SYSTEM - POWER REQUIREMENTS

Main RF Voltage	Harmonic RF Voltage	3 x 2 Harm Cav cells	4 x 2 Harm Cav cells
6.5 MV	1.49 MV	46 kW	26 kW
6.0 MV (nominal)	1.35 MV	38 kW	22 kW

Optimum harmonic cavity tuning: **Load angle = 0** (exactly as for main RF)



BEAM LOADING DIAGRAM WITH HARMONIC CAVITY FOR BUNCH LENGTHENING

$$V_{\text{acc}}(\phi) = V_c \sin(\phi_s + \phi) + V_h \sin(n\phi_h + n\phi)$$

Optimum Working point (1st & 2nd derivatives = 0):

$$\phi_s = \pi - \arcsin[n^2/(n^2-1) U_0/V_c]$$

$$V_{h,\text{opt}} = \text{sqrt}[V_c^2/n^2 - U_0^2/(n^2-1)]$$

$$\phi_{h,\text{opt}} = (1/n) \arcsin[- U_0 / (V_{h,\text{opt}} (n^2-1))]$$

Optimum tuning (min power) \Leftrightarrow load angle = 0:

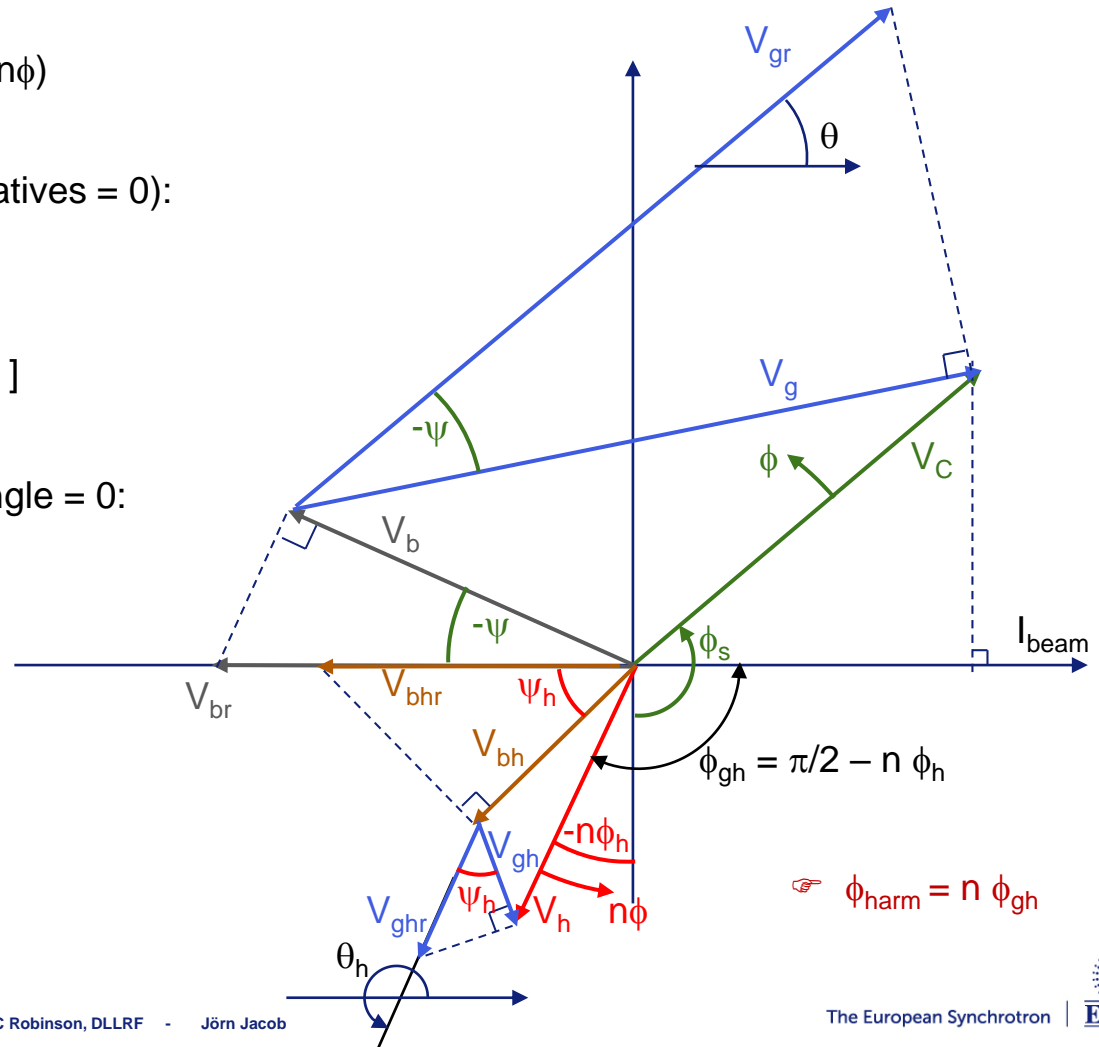
$$\psi \text{ such that } V_{\text{gr}} // V_c$$

$$\psi_h \text{ such that } V_{\text{ghr}} // V_h$$

Beware, in the vector diagram:

Main RF turns at $\phi = \omega t$

Harmonic RF at $n\phi = n\omega t$



ROBINSON DC (2ND TYPE) – INTEGRATION OF SYNCHROTRON EQUATION

Assumptions:

RF loops (Amp, Phi, tuning)	slower than	Synchrotron motion	slower than	Cavity Bandwidths (main & HC)
$B \approx 1 \text{ Hz}$	\ll	$f_s \approx 1 \text{ kHz} \dots$	\ll	Above $\approx 40 \text{ kHz}$

1. Tuning angles, generator amplitudes and phases are constant at the scale of the synchrotron motion
2. The beam induced voltages in the cavities follow the beam phase

$$f_s = f_{rf} \times \text{sqrt} [\alpha \mathbf{K}' / (2\pi h E_0/e)], \quad (\mathbf{K}' < 0 \Leftrightarrow \text{DC Robinson instability})$$

$$\mathbf{K}' = \underbrace{-V_c \cos \phi_s}_{> 0} \underbrace{- nV_h \cos(n\phi_h)}_{< 0} \underbrace{+ V_b \sin \psi}_{< 0} \underbrace{+ nV_{bh} \sin \psi_h}_{> 0} \quad (\text{Eq. 1})$$

Main RF, giving f_{s0}
Harm. RF, for cancelling f_s
Main RF beam loading (Robinson term)
Harm. RF, beam loading (Stabilizing effect)

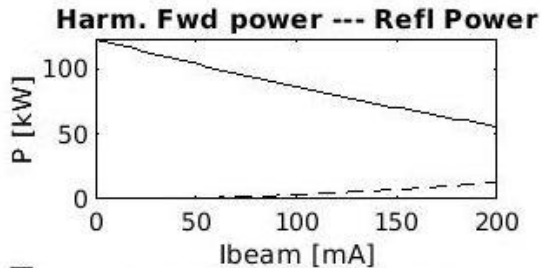
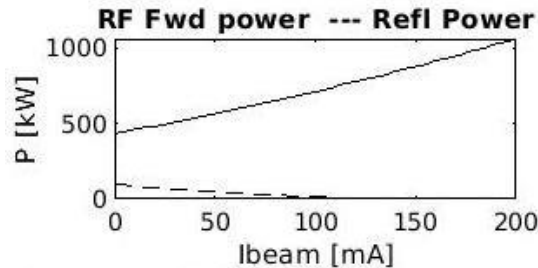
Coming examples already shown
at
ESLS RF meeting at SOLEIL in November 2018

Computed for 3rd harmonic RF system
(and not for actual 4th harmonic project)

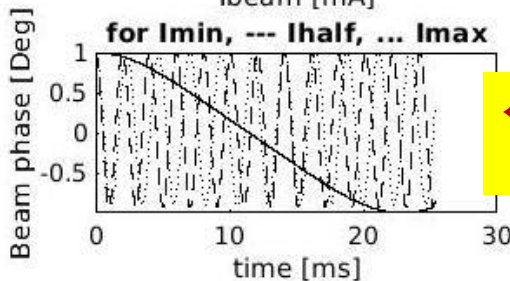
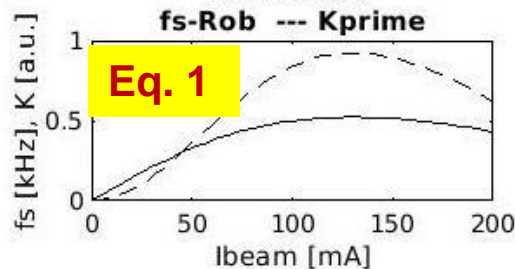
ROBINSON DC (2ND TYPE) – INTEGRATION OF SYNCHROTRON EQUATION

Numerical integration of synchrotron equation:

- Uniform filling (no transients)
- Starting with beam phase offset by +1 or -1 deg
- Tracking V_b , V_{bh} and ϕ_{beam} turn by turn
- Checking convergence (neglecting synchrotron oscillation damping)
- No linearization !

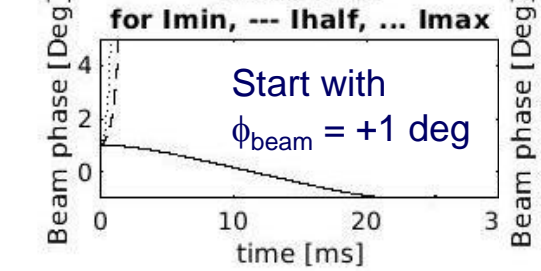
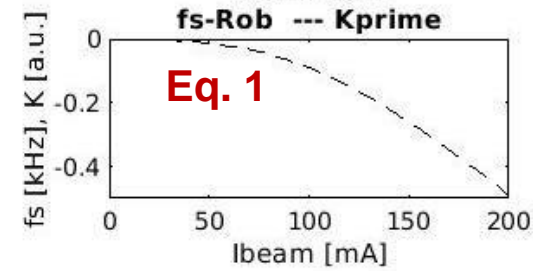
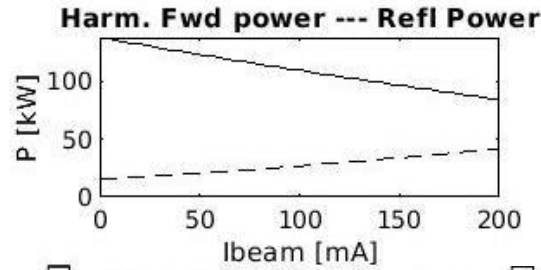
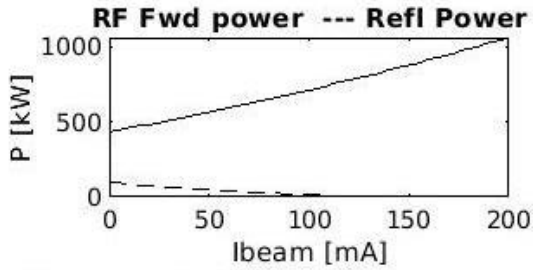


$V_h = V_{h,opt} = 1.89$ MV
 $n\phi_h = n\phi_{h,opt} = -12.2$ deg
5 cavities, $\beta_h = 1$
→ stable

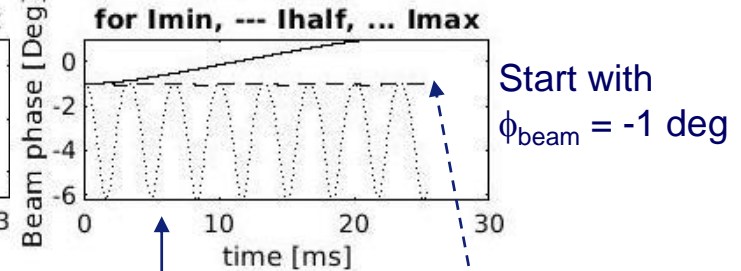


← Numerical integration

ROBINSON DC (2ND TYPE) – INTEGRATION OF SYNCHROTRON EQUATION



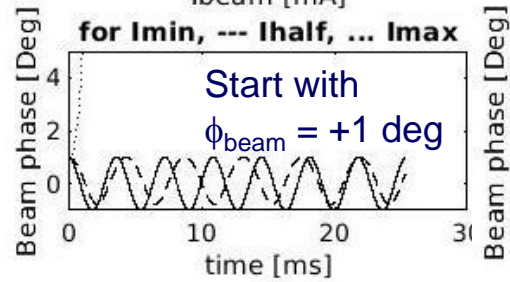
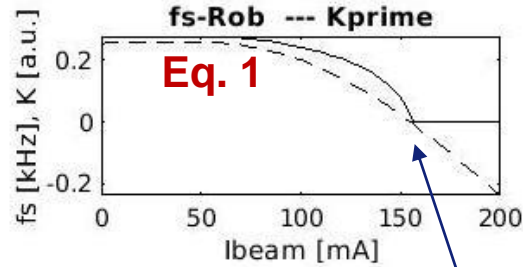
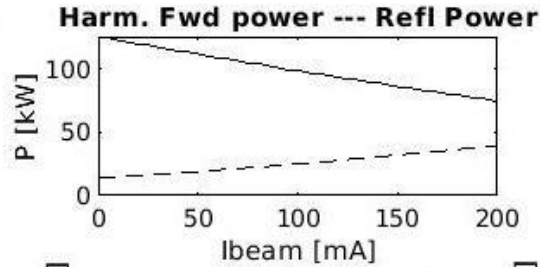
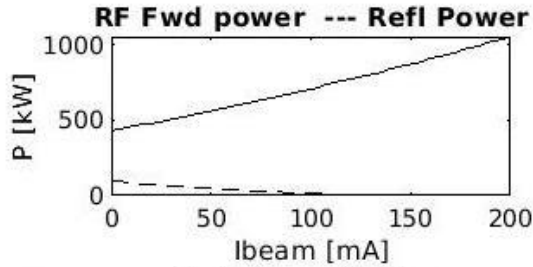
$V_h = V_{h,\text{opt}} = 1.89$ MV
 $n\phi_h = n\phi_{h,\text{opt}} = -12.2$ deg
 5 cavities, $\beta_h = 2$
 → Unstable for $I_{\text{beam}} > 0$



Only for negative beam phases: stabilization through non-linearity of voltage waveform

Equilibrium for ≈ 100 mA

ROBINSON DC (2ND TYPE) – INTEGRATION OF SYNCHROTRON EQUATION

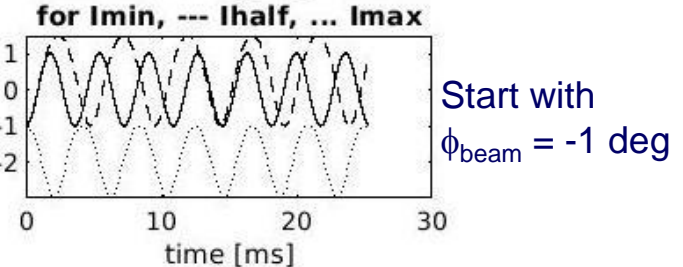


$V_h = 1.80$ MV ($\neq V_{h,\text{opt}}$)

$n\phi_h = n\phi_{h,\text{opt}} = -12.2$ deg

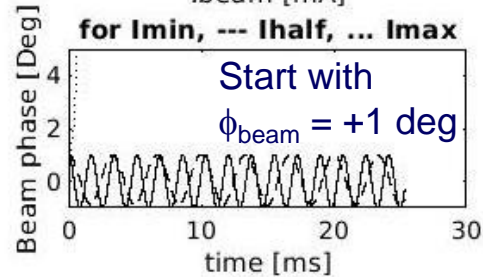
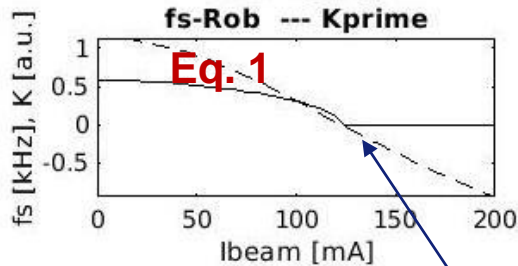
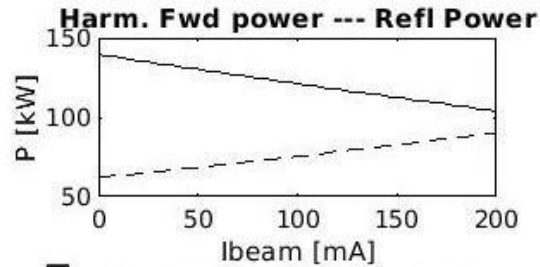
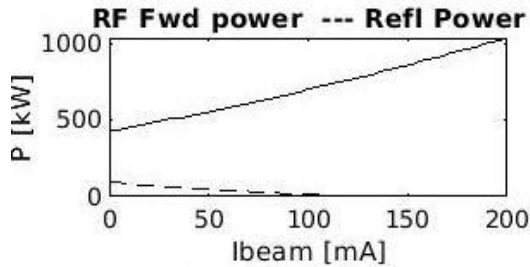
5 cavities, $\beta_h = 2$

→ Unstable for $I_{\text{beam}} > 150$ mA



Threshold at ≈ 150 mA confirmed by numerical integration

ROBINSON DC (2ND TYPE) – INTEGRATION OF SYNCHROTRON EQUATION



$V_h = 1.50 \text{ MV}$ ($\neq V_{h,\text{opt}}$)
 $n\phi_h = n\phi_{h,\text{opt}} = -12.2 \text{ deg}$
 5 cavities, $\beta_h = 5$
 → Unstable for $I_{\text{beam}} > 130 \text{ mA}$

Threshold at $\approx 130 \text{ mA}$ confirmed by numerical integration

For active system, Integration of synchrotron equation indicates:

- **Robinson stable** if Harmonic RF beam loading > Main RF beam loading
 - ⇒ Sufficient harmonic cavity impedance,
 - ⇒ Sufficient number of harmonic cavities
 - ⇒ Upper limit for coupling β_h

Analog RF feedback on MAIN RF system:

- Gain G
 - Impedance for coherent in phase longitudinal beam motion reduced by factor $1/G$
- ⇒ Reduction of Robinson term in Eq. 1 by a factor $1/G$

$$f_s = f_{rf} \times \text{sqrt} [\alpha \mathbf{K}' / (2\pi h E_0/e)], \quad (\mathbf{K}' < 0 \Leftrightarrow \text{DC Robinson instability})$$

$$\mathbf{K}' = \underbrace{-V_c \cos \phi_s}_{> 0} \underbrace{- nV_h \cos(n\phi_h)}_{< 0} \underbrace{+ V_b \sin \psi / G}_{< 0} \underbrace{+ nV_{bh} \sin \psi_h}_{> 0} \quad (\text{Eq. 1})$$

Main RF, giving f_{s0}
Harm. RF, for cancelling f_s
Main RF beam loading (Robinson term)
Harm. RF, beam loading (Stabilizing effect)

1. To stabilize main RF, one can compute the optimum correction for a fast RF feedback:

$$\begin{pmatrix} \Delta I_{gr} \\ \Delta Q_{gr} \end{pmatrix} = \frac{1}{\cos \psi} \begin{bmatrix} \cos(\psi - \varphi_{tune}) & \sin(\psi - \varphi_{tune}) \\ -\sin(\psi - \varphi_{tune}) & \cos(\psi - \varphi_{tune}) \end{bmatrix} \begin{pmatrix} \Delta I_c \\ \Delta Q_c \end{pmatrix}$$

where $\psi = f(V_c, I_{beam}, N_{cav}, R_s, \beta, \varphi_{tune})$, ($\rightarrow \varphi_{tune} = \text{Load angle, mostly zero}$)

2. Alternative: simulate behaviour of a passive cavity

- Feedback **harmonic voltage phase** to lock on **beam phase**
- Results of synchrotron equation integration need to be cross-checked with particle tracking simulations
- The two RF feedback approaches need to be included in the simulations and checked

MANY THANKS FOR YOUR ATTENTION

